

GEARTECH Report No. NOM-3

AGMA 901-A92 Annex A Example Calculations

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GEARTECH

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INPUT DATA		
Example	Janusz-1	Janusz-2
x1	0.1671	0.2727
z1		23
z2		54
Pnd		6
α_n		20
β		32.698
a _w	7.625	7.690
ΔS_n1		0.024
ΔS_n2		0.024
hao1		1.4
hao2		1.4
OUTPUT DATA		
Σx	0	0.3987
Δa	0	0.0650
x2	-0.1671	0.1260
k _s	0	0.0087
ha1	0.1945	0.2107
ha2	0.1388	0.1862
da1	4.9442	4.9765
da2	10.9724	11.0672
c1	0.0722	0.0722
c2	0.0722	0.0722
xg1	0.1341	0.2397
xg2	-0.2001	0.0930
Σg	-0.0660	0.3327
S _{n1}	0.2781	0.2909
S _{n2}	0.2375	0.2731
j _{wn}	0.0080	0.0081

Notes

1. Calculations are in accordance with AGMA 901-A92 Annex A.
2. Example Janusz-1 operates on the reference center distance $a_w = a_{ref} = 7.625$ in.
3. Example Janusz-2 operates on an increased center distance $a_w = 7.690$ in.
4. Profile shift coefficient X1 is chosen for balanced specific sliding for both examples.
5. Tip diameters are designed for standard tip-to-root clearance (option 3).

Program **Profile_shift_2** based on Appendix A of AGMA 901-A92. Use this program when tooth thicknesses s_{n1} and s_{n2} are unknown. Profile shift x_1 is a design decision and must be known. If x_1 is unknown, try iterating x_1 until the diameters agree with known values.

Input data

$x_1 := 0.1671$ Pinion profile shift
 $z_1 := 23$ Number of teeth in pinion
 $z_2 := 54$ Number of teeth in gear (negative for internal gear)
 $mn := 0.16666666666666667$ Normal module (mm) Enter mn for metric units
 Enter 1/Pn for inch units
 $\alpha_n := 20$ Normal pressure angle (deg)
 $\beta := 32.698$ Reference helix angle (deg)
 $a_w := 7.625$ Operating center distance (mm)
 $\Delta s_{n1} := 0.024$ Tooth thinning for backlash
 (normalized)
 $\Delta s_{n2} := 0.024$ Tooth thinning for backlash
 (normalized)
 $ha_o1 := 1.4$ hob addendum for pinion (normalized)
 $ha_o2 := 1.4$ hob addendum for gear (normalized)

Calculations

$\alpha_n := \alpha_n \cdot \frac{\pi}{180}$ $\beta := \beta \cdot \frac{\pi}{180}$ converts angles to radians

$s := \frac{|z_2|}{z_2}$ $s = +1$ for external gearset, -1 for internal gearset

$u := \frac{z_2}{z_1}$ Gear ratio $u = 2.34783$

$r_1 := \frac{z_1 \cdot mn}{2 \cdot \cos(\beta)}$ Pinion reference radius (mm) $r_1 = 2.2776$

$r_2 := r_1 \cdot |u|$ Wheel reference radius (mm) $r_2 = 5.34741$

$a := r_2 + s \cdot r_1$ Reference center distance (mm) $a = 7.625003763$

$rw_1 := \frac{a_w}{|u| + s}$ Pinion operating radius (mm) $rw_1 = 2.2776$

$rw_2 := rw_1 \cdot |u|$ Wheel operating radius (mm) $rw_2 = 5.3474$

$\alpha_t := \text{atan}\left(\frac{\tan(\alpha_n)}{\cos(\beta)}\right)$ Transverse reference pressure angle (rad) $\alpha_t = 0.4082147$

$rb_1 := r_1 \cdot \cos(\alpha_t)$ Pinion base radius (mm) $rb_1 = 2.09045$

$rb_2 := rb_1 \cdot |u|$ Wheel base radius (mm) $rb_2 = 4.90801$

$\alpha_{wt} := \text{acos}\left[\frac{(rb_2 + s \cdot rb_1)}{a_w}\right]$ Transverse operating pressure angle (rad) $\alpha_{wt} = 0.40821356$

Begin AGMA 901-A92 algorithm for profile shift

$\text{inv}\alpha t := \tan(\alpha t) - \alpha t$	Involute function for αt (rad)	$\text{inv}\alpha t = 0.024295597$
$\text{inv}\alpha w t := \tan(\alpha w t) - \alpha w t$	Involute function for $\alpha w t$ (rad)	$\text{inv}\alpha w t = 0.024295384$
$\Sigma x := a \cdot \frac{(\text{inv}\alpha w t - \text{inv}\alpha t)}{m n \cdot \tan(\alpha t)}$	Sum of profile shift coeffs	$\Sigma x = -2.25761 \times 10^{-5}$
$\Delta a := a_w - a$	Center distance change (mm)	$\Delta a = -3.762689397 \times 10^{-6}$
$k_s := \Sigma x - \frac{\Delta a}{m n}$	Tip shortening coefficient	$k_s = 2.97684642 \times 10^{-11}$
$x_2 := \Sigma x - s \cdot x_1$	Wheel profile shift coefficient	$x_2 = -0.167122576$
$h_{a11} := (1 + x_1) \cdot m n$	Pinion addendum full length (mm)	$h_{a11} = 0.1945$
$h_{a21} := (1 + x_2) \cdot m n$	Wheel addendum full length (mm)	$h_{a21} = 0.1388$
$h_{a12} := \left(1 + x_1 - \frac{k_s}{2}\right) \cdot m n$	Pinion addendum std working depth (mm)	$h_{a12} = 0.1945$
$h_{a22} := \left(1 + x_2 - \frac{k_s}{2}\right) \cdot m n$	Wheel addendum std working depth (mm)	$h_{a22} = 0.1388$
$h_{a13} := (1 + x_1 - k_s) \cdot m n$	Pinion addendum std tip-to-root clearance (mm)	$h_{a13} = 0.1945$
$h_{a23} := (1 + x_2 - k_s) \cdot m n$	Wheel addendum std tip-to-root clearance (mm)	$h_{a23} = 0.1388$
$r_{a11} := r_1 + h_{a11}$	Pinion tip radius full length teeth (mm)	$r_{a11} = 2.4721$
$r_{a21} := r_2 + s \cdot h_{a21}$	Wheel tip radius full length teeth (mm)	$r_{a21} = 5.4862$
$r_{a12} := r_1 + h_{a12}$	Pinion tip radius std working depth (mm)	$r_{a12} = 2.4721$
$r_{a22} := r_2 + s \cdot h_{a22}$	Wheel tip radius std working depth (mm)	$r_{a22} = 5.4862$
$r_{a13} := r_1 + h_{a13}$	Pinion tip radius std tip-to-root clearance (mm)	$r_{a13} = 2.4721$
$r_{a23} := r_2 + s \cdot h_{a23}$	Wheel tip radius std tip-to-root clearance (mm)	$r_{a23} = 5.4862$
$d_1 := 2 \cdot r_1$	$\alpha t := \alpha t \cdot \frac{180}{\pi}$	$\alpha w t := \alpha w t \cdot \frac{180}{\pi}$
$d_2 := 2 \cdot r_2$		
$d_{w1} := 2 \cdot r_{w1}$	$d_{b1} := 2 \cdot r_{b1}$	
$d_{w2} := 2 \cdot r_{w2}$	$d_{b2} := 2 \cdot r_{b2}$	
$d_{a11} := 2 \cdot r_{a11}$	$d_{a12} := 2 \cdot r_{a12}$	$d_{a13} := 2 \cdot r_{a13}$
$d_{a21} := 2 \cdot r_{a21}$	$d_{a22} := 2 \cdot r_{a22}$	$d_{a23} := 2 \cdot r_{a23}$

$xg1 := x1 - \left(\frac{\Delta sn1}{2 \cdot \tan(\alpha_n)} \right)$	Pinion generating rack shift coeff.	$xg1 = 0.1341$
$xg2 := x2 - s \cdot \left(\frac{\Delta sn2}{2 \cdot \tan(\alpha_n)} \right)$	Wheel generating rack shift coeff.	$xg2 = -0.2001$
$\Sigma xg := xg2 + s \cdot xg1$	Sum of generating rack shift coeffs	$\Sigma xg = -0.066$
$sn1 := \left[\left(\frac{\pi}{2} \right) + 2 \cdot xg1 \cdot \tan(\alpha_n) \right] \cdot mn$	Pinion tooth thinning for backlash	$sn1 = 0.2781$
$sn2 := \left[\left(\frac{\pi}{2} \right) + s \cdot 2 \cdot xg2 \cdot \tan(\alpha_n) \right] \cdot mn$	Wheel tooth thinning for backlash	$sn2 = 0.2375$
$jwn := mn \cdot (\Delta sn1 + \Delta sn2) \cdot \left(\frac{aw}{a} \right)$	Normal circular operating backlash (mm)	$jwn = 0.008$
$rf1 := r1 - (hao1 - xg1) \cdot mn$		$rf1 = 2.0666$
$rf2 := r2 - s \cdot (hao2 - s \cdot xg2) \cdot mn$		$rf2 = 5.0807$
$c11 := s \cdot (aw - rf2) - ra11$		$c11 = 0.0722$
$c21 := s \cdot (aw - ra21) - rf1$		$c21 = 0.0722$
$c12 := s \cdot (aw - rf2) - ra12$		$c12 = 0.0722$
$c22 := s \cdot (aw - ra22) - rf1$		$c22 = 0.0722$
$c13 := s \cdot (aw - rf2) - ra13$		$c13 = 0.0722$
$c23 := s \cdot (aw - ra23) - rf1$		$c23 = 0.0722$
$df1 := 2 \cdot rf1$		$df1 = 4.1332$
$df2 := 2 \cdot rf2$		$df2 = 10.1614$

Output data

Reference diameters

$d1 = 4.5552$

$d2 = 10.6948$

Operating pitch diameters

$dw1 = 4.5552$

$dw2 = 10.6948$

Base diameters

$$db1 = 4.1809$$

$$db2 = 9.816$$

Root diameters

$$df1 = 4.1332$$

$$df2 = 10.1614$$

Transverse pressure angles

$$\alpha_t = 23.388979434$$

$$\alpha_{wt} = 23.388914063$$

Profile shift coefficients

$$x1 = 0.1671$$

$$x2 = -0.1671$$

$$\Sigma x = -2.2576 \times 10^{-5}$$

Tip shortening coefficient

$$k_s = 0$$

Generating rack shift coefficients

$$x_{g1} = 0.1341$$

$$x_{g2} = -0.2001$$

$$\Sigma x_g = -0.066$$

Normal circular tooth thickness

$$s_{n1} = 0.2781$$

$$s_{n2} = 0.2375$$

Normal circular operating backlash

$$j_{wn} = 0.008$$

Tip diameters for full length teeth

$$da_{11} = 4.9442$$

$$da_{21} = 10.9724$$

Tip diameters for standard working depth

$$da12 = 4.9442$$

$$da22 = 10.9724$$

Tip diameters for standard tip-to-root clearance

$$da13 = 4.9442$$

$$da23 = 10.9724$$

Tip clearance for full length teeth

$$c11 = 0.0722$$

$$c21 = 0.0722$$

Tip clearance for standard working depth

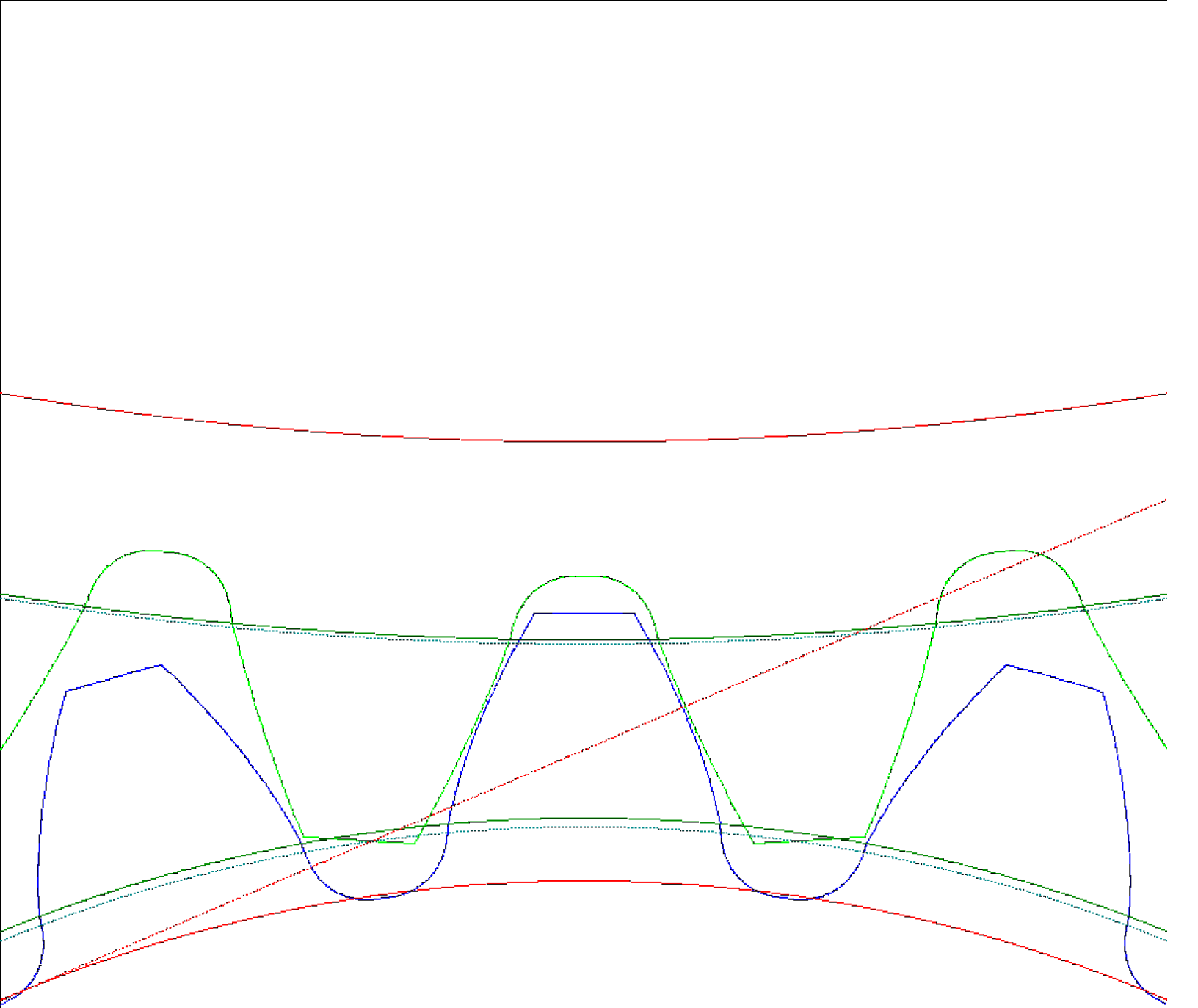
$$c12 = 0.0722$$

$$c22 = 0.0722$$

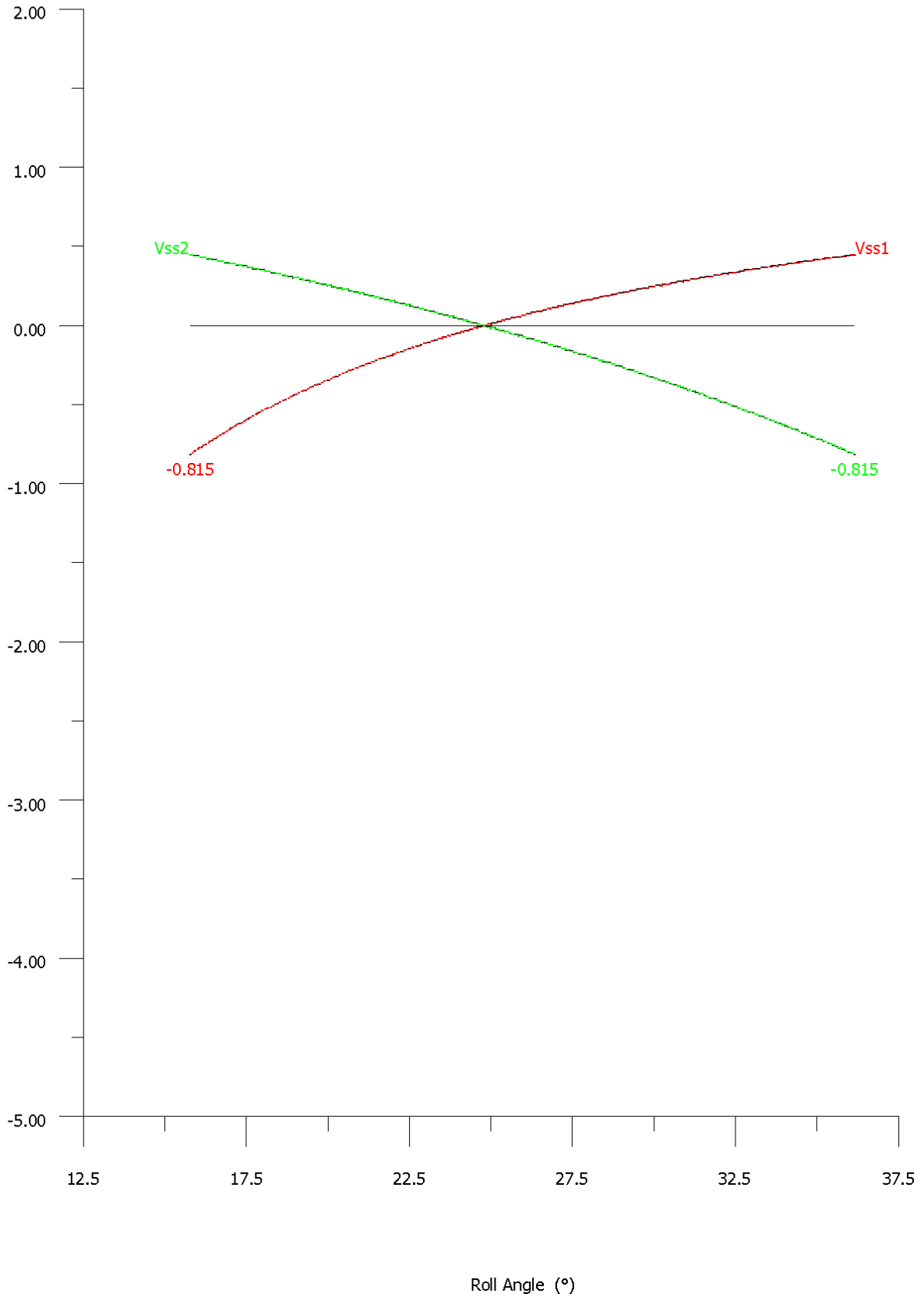
Tip clearance for standard tip-to-root clearance

$$c13 = 0.0722$$

$$c23 = 0.0722$$



Specific sliding (-)



Program **Profile_shift_2** based on Appendix A of AGMA 901-A92. Use this program when tooth thicknesses s_{n1} and s_{n2} are unknown. Profile shift x_1 is a design decision and must be known. If x_1 is unknown, try iterating x_1 until the diameters agree with known values.

Input data

$x_1 := 0.2727$	Pinion profile shift
$z_1 := 23$	Number of teeth in pinion
$z_2 := 54$	Number of teeth in gear (negative for internal gear)
$m_n := 0.16666666666666667$	Normal module (mm) Enter m_n for metric units Enter $1/P_n$ for inch units
$\alpha_n := 20$	Normal pressure angle (deg)
$\beta := 32.698$	Reference helix angle (deg)
$a_w := 7.69$	Operating center distance (mm)
$\Delta s_{n1} := 0.024$	Tooth thinning for backlash (normalized)
$\Delta s_{n2} := 0.024$	
$ha_o1 := 1.4$	hob addendum for pinion (normalized)
$ha_o2 := 1.4$	hob addendum for gear (normalized)

Calculations

$\alpha_n := \alpha_n \cdot \frac{\pi}{180}$	$\beta := \beta \cdot \frac{\pi}{180}$	converts angles to radians	
$s := \frac{ z_2 }{z_2}$	s = +1 for external gearset, -1 for internal gearset		
$u := \frac{z_2}{z_1}$	Gear ratio		u = 2.34783
$r_1 := \frac{z_1 \cdot m_n}{2 \cdot \cos(\beta)}$	Pinion reference radius (mm)		r1 = 2.2776
$r_2 := r_1 \cdot u $	Wheel reference radius (mm)		r2 = 5.34741
$a := r_2 + s \cdot r_1$	Reference center distance (mm)		a = 7.625003763
$rw_1 := \frac{a_w}{ u + s}$	Pinion operating radius (mm)		rw1 = 2.29701
$rw_2 := rw_1 \cdot u $	Wheel operating radius (mm)		rw2 = 5.39299
$\alpha_t := \text{atan}\left(\frac{\tan(\alpha_n)}{\cos(\beta)}\right)$	Transverse reference pressure angle (rad)	$\alpha_t = 0.4082147$	
$rb_1 := r_1 \cdot \cos(\alpha_t)$	Pinion base radius (mm)		rb1 = 2.09045
$rb_2 := rb_1 \cdot u $	Wheel base radius (mm)		rb2 = 4.90801
$\alpha_{wt} := \text{acos}\left[\frac{(rb_2 + s \cdot rb_1)}{a_w}\right]$	Transverse operating pressure angle (rad)	$\alpha_{wt} = 0.42733508$	

Begin AGMA 901-A92 algorithm for profile shift

$inv\alpha t := \tan(\alpha t) - \alpha t$	Involute function for αt (rad)	$inv\alpha t = 0.024295597$
$inv\alpha wt := \tan(\alpha wt) - \alpha wt$	Involute function for αwt (rad)	$inv\alpha wt = 0.028064432$
$\Sigma x := a \cdot \frac{(inv\alpha wt - inv\alpha t)}{mn \cdot \tan(\alpha t)}$	Sum of profile shift coeffs	$\Sigma x = 0.39866$
$\Delta a := a_w - a$	Center distance change (mm)	$\Delta a = 0.064996237$
$ks := \Sigma x - \frac{\Delta a}{mn}$	Tip shortening coefficient	$ks = 8.681927573 \times 10^{-3}$
$x_2 := \Sigma x - s \cdot x_1$	Wheel profile shift coefficient	$x_2 = 0.125959351$
$ha_{11} := (1 + x_1) \cdot mn$	Pinion addendum full length (mm)	$ha_{11} = 0.2121$
$ha_{21} := (1 + x_2) \cdot mn$	Wheel addendum full length (mm)	$ha_{21} = 0.1877$
$ha_{12} := \left(1 + x_1 - \frac{ks}{2}\right) \cdot mn$	Pinion addendum std working depth (mm)	$ha_{12} = 0.2114$
$ha_{22} := \left(1 + x_2 - \frac{ks}{2}\right) \cdot mn$	Wheel addendum std working depth (mm)	$ha_{22} = 0.1869$
$ha_{13} := (1 + x_1 - ks) \cdot mn$	Pinion addendum std tip-to-root clearance (mm)	$ha_{13} = 0.2107$
$ha_{23} := (1 + x_2 - ks) \cdot mn$	Wheel addendum std tip-to-root clearance (mm)	$ha_{23} = 0.1862$
$ra_{11} := r_1 + ha_{11}$	Pinion tip radius full length teeth (mm)	$ra_{11} = 2.4897$
$ra_{21} := r_2 + s \cdot ha_{21}$	Wheel tip radius full length teeth (mm)	$ra_{21} = 5.5351$
$ra_{12} := r_1 + ha_{12}$	Pinion tip radius std working depth (mm)	$ra_{12} = 2.489$
$ra_{22} := r_2 + s \cdot ha_{22}$	Wheel tip radius std working depth (mm)	$ra_{22} = 5.5343$
$ra_{13} := r_1 + ha_{13}$	Pinion tip radius std tip-to-root clearance (mm)	$ra_{13} = 2.4883$
$ra_{23} := r_2 + s \cdot ha_{23}$	Wheel tip radius std tip-to-root clearance (mm)	$ra_{23} = 5.5336$
$d_1 := 2 \cdot r_1$	$\alpha t := \alpha t \cdot \frac{180}{\pi}$	$\alpha wt := \alpha wt \cdot \frac{180}{\pi}$
$d_2 := 2 \cdot r_2$		
$dw_1 := 2 \cdot rw_1$	$db_1 := 2 \cdot rb_1$	
$dw_2 := 2 \cdot rw_2$	$db_2 := 2 \cdot rb_2$	
$da_{11} := 2 \cdot ra_{11}$	$da_{12} := 2 \cdot ra_{12}$	$da_{13} := 2 \cdot ra_{13}$
$da_{21} := 2 \cdot ra_{21}$	$da_{22} := 2 \cdot ra_{22}$	$da_{23} := 2 \cdot ra_{23}$

$xg1 := x1 - \left(\frac{\Delta sn1}{2 \cdot \tan(\alpha_n)} \right)$	Pinion generating rack shift coeff.	$xg1 = 0.2397$
$xg2 := x2 - s \cdot \left(\frac{\Delta sn2}{2 \cdot \tan(\alpha_n)} \right)$	Wheel generating rack shift coeff.	$xg2 = 0.093$
$\Sigma xg := xg2 + s \cdot xg1$	Sum of generating rack shift coeffs	$\Sigma xg = 0.3327$
$sn1 := \left[\left(\frac{\pi}{2} \right) + 2 \cdot xg1 \cdot \tan(\alpha_n) \right] \cdot mn$	Pinion tooth thinning for backlash	$sn1 = 0.2909$
$sn2 := \left[\left(\frac{\pi}{2} \right) + s \cdot 2 \cdot xg2 \cdot \tan(\alpha_n) \right] \cdot mn$	Wheel tooth thinning for backlash	$sn2 = 0.2731$
$jwn := mn \cdot (\Delta sn1 + \Delta sn2) \cdot \left(\frac{aw}{a} \right)$	Normal circular operating backlash (mm)	$jwn = 0.0081$
$rf1 := r1 - (hao1 - xg1) \cdot mn$	$rf1 = 2.0842$	
$rf2 := r2 - s \cdot (hao2 - s \cdot xg2) \cdot mn$	$rf2 = 5.1296$	
$c11 := s \cdot (aw - rf2) - ra11$	$c11 = 0.0707$	
$c21 := s \cdot (aw - ra21) - rf1$	$c21 = 0.0707$	
$c12 := s \cdot (aw - rf2) - ra12$	$c12 = 0.0714$	
$c22 := s \cdot (aw - ra22) - rf1$	$c22 = 0.0714$	
$c13 := s \cdot (aw - rf2) - ra13$	$c13 = 0.0722$	
$c23 := s \cdot (aw - ra23) - rf1$	$c23 = 0.0722$	
$df1 := 2 \cdot rf1$	$df1 = 4.1684$	
$df2 := 2 \cdot rf2$	$df2 = 10.2591$	

Output data

Reference diameters

$d1 = 4.5552$

$d2 = 10.6948$

Operating pitch diameters

$dw1 = 4.594$

$dw2 = 10.786$

Base diameters

$$db1 = 4.1809$$

$$db2 = 9.816$$

Root diameters

$$df1 = 4.1684$$

$$df2 = 10.2591$$

Transverse pressure angles

$$\alpha_t = 23.388979434$$

$$\alpha_{wt} = 24.484496538$$

Profile shift coefficients

$$x1 = 0.2727$$

$$x2 = 0.126$$

$$\Sigma x = 0.3987$$

Tip shortening coefficient

$$ks = 0.0087$$

Generating rack shift coefficients

$$xg1 = 0.2397$$

$$xg2 = 0.093$$

$$\Sigma xg = 0.3327$$

Normal circular tooth thickness

$$sn1 = 0.2909$$

$$sn2 = 0.2731$$

Normal circular operating backlash

$$j_{wn} = 0.0081$$

Tip diameters for full length teeth

$$da11 = 4.9794$$

$$da21 = 11.0701$$

Tip diameters for standard working depth

$$da12 = 4.978$$

$$da22 = 11.0687$$

Tip diameters for standard tip-to-root clearance

$$da13 = 4.9765$$

$$da23 = 11.0672$$

Tip clearance for full length teeth

$$c11 = 0.0707$$

$$c21 = 0.0707$$

Tip clearance for standard working depth

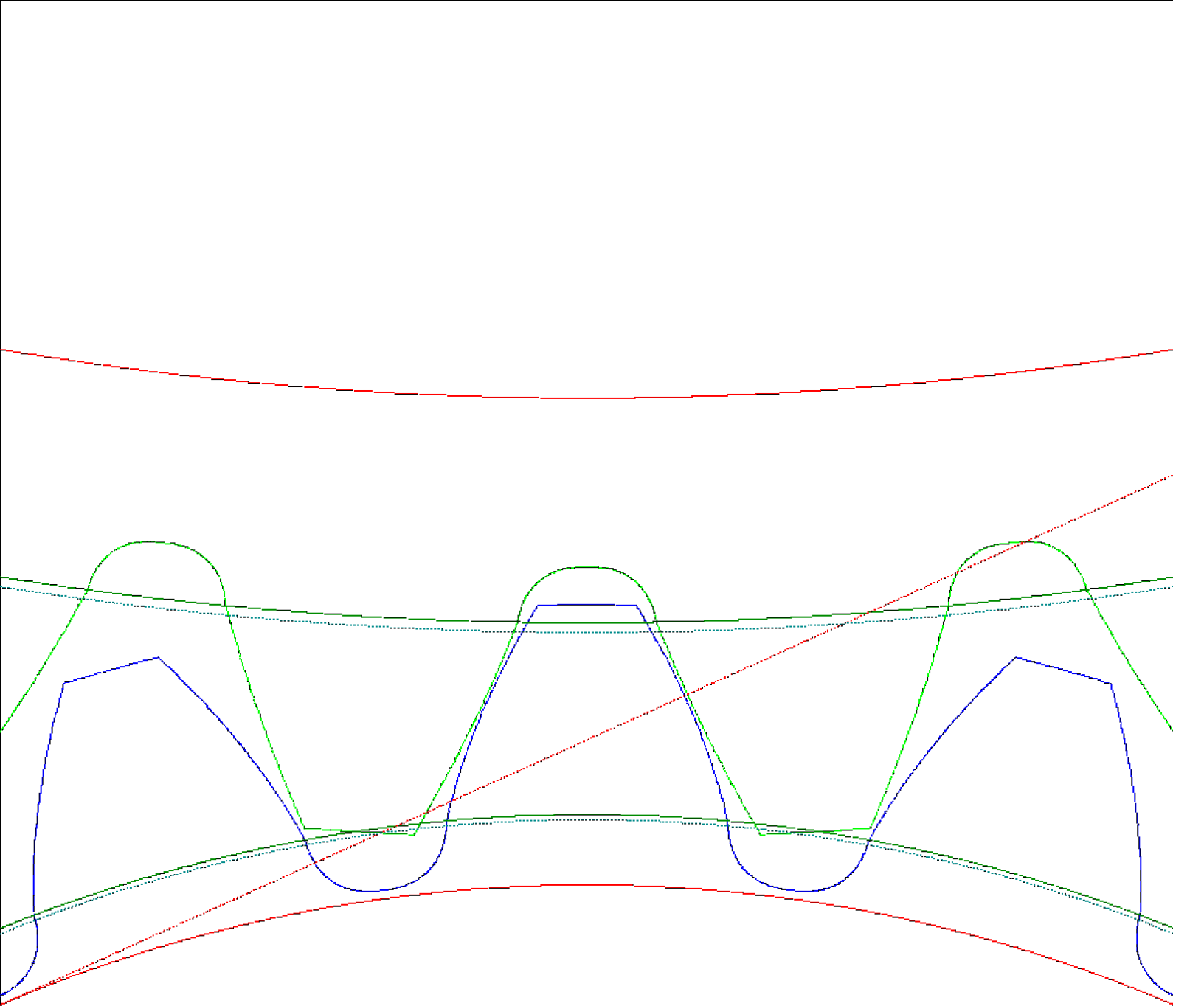
$$c12 = 0.0714$$

$$c22 = 0.0714$$

Tip clearance for standard tip-to-root clearance

$$c13 = 0.0722$$

$$c23 = 0.0722$$



Specific sliding (-)

